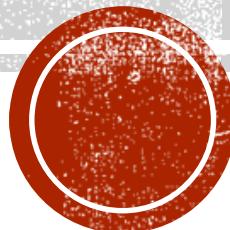


# **SPECIAL PRODUCTS**

**Lesson 7.4**



Some pairs of binomials show patterns when multiplied. You can use these patterns to multiply other similar pairs of binomials.

## SPECIAL PRODUCT PATTERNS

Sum and Difference Pattern aka the Difference of Squares

$$(a + b)(a - b)$$



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Example:  $(3x + 4)(3x - 4)$   
 $= 9x^2 \boxed{- 12x} + \boxed{12x} - 16$

Notice that the middle term is zero.



**EXAMPLE****1****Using the Sum and Difference Pattern**

Find each product.

a.  $(x + 7)(x - 7)$

b.  $(3x - 1)(3x + 1)$

**EXAMPLE** **1** Using the Sum and Difference Pattern

Find each product.

a.  $(x + 7)(x - 7)$

$$(a + b)(a - b) = a^2 - b^2 \quad \text{Sum and Difference Pattern}$$

b.  $(3x - 1)(3x + 1)$

**EXAMPLE****1****Using the Sum and Difference Pattern**

Find each product.

a.  $(x + 7)(x - 7)$

$$(\textcolor{red}{a} + \textcolor{blue}{b})(\textcolor{red}{a} - \textcolor{blue}{b}) = \textcolor{red}{a}^2 - \textcolor{blue}{b}^2$$

Sum and Difference Pattern

$$(\textcolor{red}{x} + 7)(\textcolor{red}{x} - 7) = \textcolor{red}{x}^2 - 7^2$$

Use pattern.

b.  $(3x - 1)(3x + 1)$

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Sum and Difference Pattern

$$(\textcolor{red}{x} + 7)(\textcolor{red}{x} - 7) = \textcolor{red}{x}^2 - 7^2$$

Use pattern.

$$= x^2 - 49$$

Simplify.

b.  $(3x - 1)(3x + 1)$

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Sum and Difference Pattern

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Sum and Difference Pattern

$$(\textcolor{red}{3x} - 1)(\textcolor{red}{3x} + 1) = (\textcolor{red}{3x})^2 - 1^2$$

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Sum and Difference Pattern

$$(\textcolor{red}{3x} - 1)(\textcolor{red}{3x} + 1) = (\textcolor{red}{3x})^2 - 1^2$$

Use pattern.

$$= 9x^2 - 1$$

Simplify.



## On Your Own

Find the product.

$$1. \quad (x - 4)(x + 4)$$

$$= x^2 - 16$$

$$2. \quad (b + 10)(b - 10)$$

$$= b^2 - 100$$

$$3. \quad (2g + 5)(2g - 5)$$

$$= 4g^2 - 25$$



Some pairs of binomials show patterns when multiplied. You can use these patterns to multiply other similar pairs of binomials.

## SPECIAL PRODUCT PATTERNS

### Square of Binomial Pattern

$$(a + b)^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = a^2 - 2ab + b^2$$



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### Square of Binomial Pattern

$$(a + b)^2 = a^2 + 2ab + b^2 \quad \text{Example: } (x + 5)^2 = x^2 + 10x + 25$$

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### Square of Binomial Pattern

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$$(a - b)^2 = a^2 - 2ab + b^2 \quad \text{Example: } (2x - 3)^2 = 4x^2 - 12x + 9$$

Notice that the middle term is twice the product of the terms of the binomial.



**EXAMPLE 2** Using the Square of a Binomial Pattern

Find each product.

a.  $(y + 1)^2$

b.  $(2z - 3)^2$

**EXAMPLE** **2** Using the Square of a Binomial Pattern

Find each product.

a.  $(y + 1)^2$

$$(a + b)^2 = a^2 + 2ab + b^2 \quad \text{Square of a Binomial Pattern}$$

b.  $(2z - 3)^2$

**EXAMPLE 2** Using the Square of a Binomial Pattern

Find each product.

a.  $(y + 1)^2$

$$(a + b)^2 = a^2 + 2ab + b^2 \quad \text{Square of a Binomial Pattern}$$

$$(y + 1)^2 = y^2 + 2(y)(1) + 1^2 \quad \text{Use pattern.}$$

b.  $(2z - 3)^2$

**EXAMPLE 2** Using the Square of a Binomial Pattern

Find each product.

a.  $(y + 1)^2$

$$(a + b)^2 = a^2 + 2ab + b^2 \quad \text{Square of a Binomial Pattern}$$

$$\begin{aligned} (y + 1)^2 &= y^2 + 2(y)(1) + 1^2 && \text{Use pattern.} \\ &= y^2 + 2y + 1 && \text{Simplify.} \end{aligned}$$

b.  $(2z - 3)^2$

**EXAMPLE****2****Using the Square of a Binomial Pattern**

**Find each product.**

a.  $(y + 1)^2$

$$(\textcolor{red}{a} + \textcolor{blue}{b})^2 = \textcolor{red}{a}^2 + 2\textcolor{red}{a}\textcolor{blue}{b} + \textcolor{blue}{b}^2$$

Square of a Binomial Pattern

$$(\textcolor{red}{y} + \textcolor{blue}{1})^2 = \textcolor{red}{y}^2 + 2(\textcolor{red}{y})(\textcolor{blue}{1}) + \textcolor{blue}{1}^2$$

Use pattern.

$$= y^2 + 2y + 1$$

Simplify.

b.  $(2z - 3)^2$

$$(\textcolor{red}{a} - \textcolor{blue}{b})^2 = \textcolor{red}{a}^2 - 2\textcolor{red}{a}\textcolor{blue}{b} + \textcolor{blue}{b}^2$$

Square of a Binomial Pattern

**EXAMPLE****2****Using the Square of a Binomial Pattern**

**Find each product.**

a.  $(y + 1)^2$

$$(\textcolor{red}{a} + \textcolor{blue}{b})^2 = \textcolor{red}{a}^2 + 2\textcolor{red}{a}\textcolor{blue}{b} + \textcolor{blue}{b}^2$$

Square of a Binomial Pattern

$$(\textcolor{red}{y} + 1)^2 = \textcolor{red}{y}^2 + 2(\textcolor{red}{y})(1) + 1^2$$

Use pattern.

$$= y^2 + 2y + 1$$

Simplify.

b.  $(2z - 3)^2$

$$(\textcolor{red}{a} - \textcolor{blue}{b})^2 = \textcolor{red}{a}^2 - 2\textcolor{red}{a}\textcolor{blue}{b} + \textcolor{blue}{b}^2$$

Square of a Binomial Pattern

$$(\textcolor{red}{2z} - 3)^2 = (\textcolor{red}{2z})^2 - 2(\textcolor{red}{2z})(3) + 3^2$$

Use pattern.

**EXAMPLE** **2** Using the Square of a Binomial Pattern

Find each product.

a.  $(y + 1)^2$

$$(a + b)^2 = a^2 + 2ab + b^2$$

Square of a Binomial Pattern

$$(y + 1)^2 = y^2 + 2(y)(1) + 1^2$$

Use pattern.

$$= y^2 + 2y + 1$$

Simplify.

b.  $(2z - 3)^2$

$$(a - b)^2 = a^2 - 2ab + b^2$$

Square of a Binomial Pattern

$$(2z - 3)^2 = (2z)^2 - 2(2z)(3) + 3^2$$

Use pattern.

$$= 4z^2 - 12z + 9$$

Simplify.



## On Your Own

Find the product.

$$4. \quad (w + 2)^2$$

$$= w^2 + 4w + 4$$

$$5. \quad (x - 7)^2$$

$$= x^2 - 14x + 49$$

$$6. \quad (3y - 1)^2$$

$$= 9y^2 - 6y + 1$$

$$7. \quad (5z + 4)^2$$

$$= 25z^2 + 40z + 16$$

