

Dividing Polynomials

11.5

Dividing a Polynomial by a Monomial

- Divide each term in the polynomial by the monomial.

a. $3s^2 + 3s - 9 \div 3s$

$$\frac{3s^2}{3s} + \frac{3s}{3s} - \frac{9}{3s}$$

b. $4x^2 - 6x + 8 \div 2x$

Dividing a Polynomial by a Monomial

- Divide each term in the polynomial by the monomial.

a. $3s^2 + 3s - 9 \div 3s$

$$\frac{\cancel{s} \cancel{3s^2}}{1 \cancel{3s}} + \frac{3s}{3s} - \frac{9}{3s}$$

b. $4x^2 - 6x + 8 \div 2x$

Dividing a Polynomial by a Monomial

- Divide each term in the polynomial by the monomial.

a. $3s^2 + 3s - 9 \div 3s$

$$\begin{array}{r} s \cancel{3s^2} \\ 1 \cancel{3s} \end{array} + \frac{\cancel{3s}1}{\cancel{3s}1} - \frac{9}{3s}$$

b. $4x^2 - 6x + 8 \div 2x$

Dividing a Polynomial by a Monomial

- Divide each term in the polynomial by the monomial.

a. $3s^2 + 3s - 9 \div 3s$

$$\frac{s \cancel{3s^2}}{1 \cancel{3s}} + \frac{\cancel{3s}1}{\cancel{3s}1} - \frac{\cancel{9}3}{\cancel{3s}s}$$

$$s + 1 - \frac{3}{s}$$

b. $4x^2 - 6x + 8 \div 2x$

$$\frac{4x^2}{2x} - \frac{6x}{2x} + \frac{8}{2x}$$

Dividing a Polynomial by a Monomial

- Divide each term in the polynomial by the monomial.

a. $3s^2 + 3s - 9 \div 3s$

$$\begin{array}{r} s \cancel{3s^2} \\ \hline 1 \cancel{3s} \end{array} + \begin{array}{r} \cancel{3s} 1 \\ \hline \cancel{3s} 1 \end{array} - \begin{array}{r} \cancel{9} 3 \\ \hline \cancel{3s} s \end{array}$$

$$s + 1 - \frac{3}{s}$$

b. $4x^2 - 6x + 8 \div 2x$

$$\begin{array}{r} 2x \cancel{4x^2} \\ \hline 1 \cancel{2x} \end{array} - \frac{6x}{2x} + \frac{8}{2x}$$

Dividing a Polynomial by a Monomial

- Divide each term in the polynomial by the monomial.

a. $3s^2 + 3s - 9 \div 3s$

$$\begin{array}{r} s \cancel{3s^2} \\ \hline 1 \cancel{3s} \end{array} + \begin{array}{r} \cancel{3s} 1 \\ \hline \cancel{3s} 1 \end{array} - \begin{array}{r} \cancel{9} 3 \\ \hline \cancel{3s} s \end{array}$$

$$s + 1 - \frac{3}{s}$$

b. $4x^2 - 6x + 8 \div 2x$

$$\begin{array}{r} 2x \cancel{4x^2} \\ \hline 1 \cancel{2x} \end{array} - \begin{array}{r} \cancel{6x} 3 \\ \hline \cancel{2x} 1 \end{array} + \frac{8}{2x}$$

Dividing a Polynomial by a Monomial

- Divide each term in the polynomial by the monomial.

a. $3s^2 + 3s - 9 \div 3s$

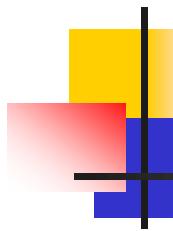
$$\begin{array}{r} s \cancel{3s^2} \\ \hline 1 \cancel{3s} \end{array} + \begin{array}{r} \cancel{3s} 1 \\ \hline \cancel{3s} 1 \end{array} - \begin{array}{r} \cancel{9} 3 \\ \hline \cancel{3s} s \end{array}$$

$$s + 1 - \frac{3}{s}$$

b. $4x^2 - 6x + 8 \div 2x$

$$\begin{array}{r} 2x \cancel{4x^2} \\ \hline 1 \cancel{2x} \end{array} - \begin{array}{r} \cancel{6x} 3 \\ \hline \cancel{2x} 1 \end{array} + \begin{array}{r} \cancel{8} 4 \\ \hline \cancel{2x} x \end{array}$$

$$2x - 3 + \frac{4}{x}$$



On Your Own

Find the quotient.

$$1. \ (4z^2 - 18z) \div 2z \qquad \qquad 2z - 9$$

$$2. \ (n^2 - 4n + 8) \div n \qquad \qquad n - 4 + \frac{8}{n}$$

$$3. \ (y^3 - 4y^2 + 9y) \div 4y \qquad \frac{y^2}{4} - y + \frac{9}{4}$$

Dividing a Polynomial by a Binomial: No Remainder

- You can use long division to divide a polynomial by a binomial.
Find $(s^2 - 2s - 8) \div (s + 2)$.

Step 1: Divide the first term of dividend by first term of the divisor.

$$\begin{array}{r} s \\ s+2 \overline{)s^2 - 2s - 8} \\ -(s^2 + 2s) \\ \hline -4s - 8 \end{array}$$

Divide: $s^2 \div s = s$

Multiply: $s(s + 2)$

Subtract. Bring down -8

Step 2: Divide the first term of $-4s - 8$ by first term of the divisor.

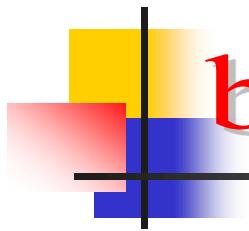
$$\begin{array}{r} s - 4 \\ s+2 \overline{)s^2 - 2s - 8} \\ -(s^2 + 2s) \\ \hline -4s - 8 \\ -(-4s - 8) \\ \hline 0 \end{array}$$

Multiply: $-4(s + 2)$
Subtract.

Dividing a Polynomial by a Binomial: No Remainder

- You could have also factored out $s^2 - 2s - 8$ and divided out a common factor.

$$\frac{(s-4)(s+2)}{s+2} = s-4$$



Dividing a Polynomial by a Binomial: Remainder

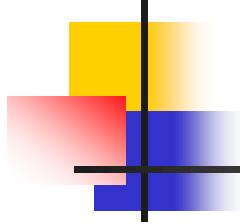
When you use long division to divide polynomials and you obtain a nonzero remainder, use the following rule.

$$\text{Dividend} \div \text{Divisor} = \text{Quotient} + \frac{\text{Remainder}}{\text{Divisor}}$$

Find $(2 - 7y + y^2) \div (y - 3)$.

$$\begin{array}{r} y - 4 \\ \hline y - 3) y^2 - 7y + 2 \\ \underline{- (y^2 - 3y)} \\ \hline -4y + 2 \\ \underline{- (-4y + 12)} \\ \hline -10 \end{array}$$

$$\text{So, } (2 - 7y + y^2) \div (y - 3) = y - 4 - \frac{10}{y - 3}.$$

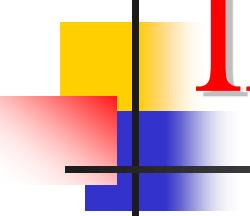


On Your Own

Find the quotient.

4. $(s^2 - 3s - 28) \div (s - 7)$ *s + 4*

5. $(x^2 + 4x - 5) \div (2 + x)$ *x + 2 - \frac{9}{x + 2}*



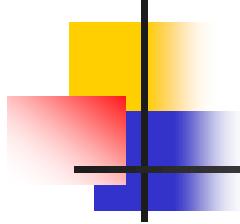
Inserting a Missing Term

- When dividing polynomials using long division, first write the polynomials in standard form and insert any missing terms..

Find $(2s^2 - 4) \div (s - 2)$.

$$\begin{array}{r} 2s + 4 \\ s - 2 \overline{)2s^2 + 0s - 4} \\ \underline{- (2s^2 - 4s)} \\ 4s - 4 \\ \underline{- (4s - 8)} \\ 4 \end{array}$$

$$\text{So, } (2s^2 - 4) \div (s - 2) = 2s + 4 + \frac{4}{s-2}$$



On Your Own

Find the quotient.

6. $(z^2 + 6) \div (z + 9)$
$$z - 9 + \frac{87}{z + 9}$$

7. $(9y^2 - 4) \div (3y + 2)$
$$3y - 2$$