## PERCENTS OF INCREASE AND DECREASE <br> Lesson 6.5

-Percents can be used to describe how an amount changes.
-This is used to compare differences of increases or decreases. For example, the price of gasoline has decreased from $\$ 4.00 / \mathrm{gal}$. to $\$ 2.00$ per gallon. The average price of homes has decreased from $\$ 500,000$ to $\$ 425,000$. Which has decreased more?

## EXAMPLE

-Many people might say that the prices of homes have decreased more than the price of gas. The homes have decreased by $\$ 75,000$ and the gas has decreased by $\$ 2$. However, we need to consider what we are comparing.
-Homes are very expensive in relation to gasoline. We are comparing two very different things.

## EXAMPLE

-There is a formula we can use to calculate the percent of change. Then we can compare the two different items.

A percent of change is the percent that a quantity changes from the original amount.

$$
\text { percent of change }=\frac{\text { amount of change }}{\text { original amount }}
$$

## EXAMPLE

Now let's look at the home and gasoline prices.

$$
\% \text { of change }=\frac{\text { amount of change }}{\text { original amount }}
$$

The house prices went from $\$ 500,000$ to $\$ 425,000$.
$=\frac{500,000-425,000}{500,000}$
$=\frac{75,000}{500,000}$
$=0.15$
= $15 \%$

The gas prices went from
\$4 to \$2.
$=\frac{4-2}{4}$
$=\frac{2}{4}$
$=0.5$
$=50 \%$

## Percents of Increase and Decrease

When the original amount increases, the percent of change is called a percent of increase.

$$
\text { percent of increase }=\frac{\text { new amount }- \text { original amount }}{\text { original amount }}
$$

When the original amount decreases, the percent of change is called a percent of decrease.

$$
\text { percent of decrease }=\frac{\text { original amount }- \text { new amount }}{\text { original amount }}
$$

## EXAMPLE 1 Finding a Percent of Increase

The table shows the numbers of hours you spent online last weekend. What is the percent of change in your online time from Saturday to Sunday?

| Day | Hours Online |
| :---: | :---: |
| Saturday | 2 |
| Sunday | 4.5 |

The number of hours on Sunday is greater than the number of hours on Saturday. So, the percent of change is a percent of increase.

## EXAMPLE q Finding a Percent of Increase

The table shows the numbers of hours you spent online last weekend. What is the percent of change in your online time from Saturday to Sunday?

| Day | Hours Online |
| :---: | :---: |
| Saturday | 2 |
| Sunday | 4.5 |

The number of hours on Sunday is greater than the number of hours on Saturday. So, the percent of change is a percent of increase.

$$
\text { percent of increase }=\frac{\text { new amount }- \text { original amount }}{\text { original amount }}
$$

## EXAMPLE 1 Finding a Percent of Increase

The table shows the numbers of hours you spent online last weekend. What is the percent of change in your online time from Saturday to Sunday?

| Day | Hours Online |
| :---: | :---: |
| Saturday | 2 |
| Sunday | 4.5 |

The number of hours on Sunday is greater than the number of hours on Saturday. So, the percent of change is a percent of increase.

$$
\begin{aligned}
\text { percent of increase } & =\frac{\text { new amount }- \text { original amount }}{\text { original amount }} \\
& =\frac{4.5-2}{2} \quad \text { Substitute. }
\end{aligned}
$$

## EXAMPLE

## 1 Finding a Percent of Increase

The table shows the numbers of hours you spent online last weekend. What is the percent of change in your online time from Saturday to Sunday?

| Day | Hours Online |
| :---: | :---: |
| Saturday | 2 |
| Sunday | 4.5 |

The number of hours on Sunday is greater than the number of hours on Saturday. So, the percent of change is a percent of increase.

$$
\begin{array}{rlr}
\text { percent of increase } & =\frac{\text { new amount }- \text { original amount }}{\text { original amount }} \\
& =\frac{4.5-2}{2} & \text { Substitute. } \\
& =\frac{2.5}{2} & \text { Subtract. }
\end{array}
$$

## 9 Finding a Percent of Increase

The table shows the numbers of hours you spent online last weekend. What is the percent of change in your online time from Saturday to Sunday?

| Day | Hours Online |
| :---: | :---: |
| Saturday | 2 |
| Sunday | 4.5 |

The number of hours on Sunday is greater than the number of hours on Saturday. So, the percent of change is a percent of increase.

$$
\begin{array}{rlr}
\text { percent of increase } & =\frac{\text { new amount }- \text { original amount }}{\text { original amount }} \\
& =\frac{4.5-2}{2} & \text { Substitute. } \\
& =\frac{2.5}{2} & \text { Subtract. } \\
& =1.25, \text { or } 125 \% & \text { Write as a percent. }
\end{array}
$$

$\therefore$ So, your online time increased $125 \%$ from Saturday to Sunday.

## On Your Own

Find the percent of change. Round to the nearest tenth of a percent if necessary.

1. 10 inches to 25 inches
2. 57 people to 65 people

## EXAMPLE 2 Finding a Percent of Decrease

The bar graph shows a softball player's home run totals. What was the percent of change from 2012 to 2013 ?


The number of home runs decreased from 2012 to 2013. So, the percent of change is a percent of decrease.
percent of decrease $=\frac{\text { original amount }- \text { new amount }}{\text { original amount }}$

## EXAMPLE 2 Finding a Percent of Decrease

The bar graph shows a softball player's home run totals. What was the percent of change from 2012 to 2013 ?


The number of home runs decreased from 2012 to 2013. So, the percent of change is a percent of decrease.
percent of decrease $=\frac{\text { original amount }- \text { new amount }}{\text { original amount }}$

$$
=\frac{28-20}{28} \quad \text { Substitute. }
$$

## EXAMPLE 2 Finding a Percent of Decrease

The bar graph shows a softball player's home run totals. What was the percent of change from 2012 to 2013 ?


The number of home runs decreased from 2012 to 2013. So, the percent of change is a percent of decrease.
percent of decrease $=\frac{\text { original amount }- \text { new amount }}{\text { original amount }}$

$$
\begin{array}{ll}
=\frac{28-20}{28} & \text { Substitute. } \\
=\frac{8}{28} & \text { Subtract. }
\end{array}
$$

## EXAMPLE 2 Finding a Percent of Decrease

The bar graph shows a softball player's home run totals. What was the percent of change from 2012 to 2013 ?


The number of home runs decreased from 2012 to 2013. So, the percent of change is a percent of decrease.
percent of decrease $=\frac{\text { original amount }- \text { new amount }}{\text { original amount }}$

$$
\begin{array}{ll}
=\frac{28-20}{28} & \text { Substitute. } \\
=\frac{8}{28} & \text { Subtract. }
\end{array}
$$

$$
\approx 0.286, \text { or } 28.6 \%
$$

Write as a percent.
$\therefore$ So, the number of home runs decreased about $28.6 \%$.

## EXAMPLE 3 Finding a Percent Error

You estimate that the length of your classroom is 16 feet. The actual length is 21 feet. Find the percent error.

The amount of error is $21-16=5$ feet.

## EXAMPLE 3 Finding a Percent Error

You estimate that the length of your classroom is 16 feet. The actual length is 21 feet. Find the percent error.

The amount of error is $21-16=5$ feet.
percent error $=\frac{\text { amount of error }}{\text { actual amount }} \quad$ Write percent error equation.

## EXAMPLE 3 Finding a Percent Error

You estimate that the length of your classroom is 16 feet. The actual length is 21 feet. Find the percent error.

The amount of error is $21-16=5$ feet.

$$
\begin{aligned}
\text { percent error } & =\frac{\text { amount of error }}{\text { actual amount }} & & \text { Write percent error equation. } \\
& =\frac{5}{21} & & \text { Substitute. }
\end{aligned}
$$

## EXAMPLE 3 Finding a Percent Error

You estimate that the length of your classroom is 16 feet. The actual length is 21 feet. Find the percent error.

The amount of error is $21-16=5$ feet.

$$
\begin{aligned}
\text { percent error } & =\frac{\text { amount of error }}{\text { actual amount }} & & \text { Write percent error equation. } \\
& =\frac{5}{21} & & \text { Substitute. } \\
& \approx 0.238, \text { or } 23.8 \% & & \text { Write as a percent. }
\end{aligned}
$$

:- The percent error is about $23.8 \%$.

